Evaluation of Lateglacial temperatures in the Southern Alps of New Zealand based on glacier modelling at Irishman Stream, Ben Ohau Range

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Article info
Article history:
Received 5 February 2012
Received in revised form 6 September 2012
Accepted 12 September 2012
Available online 6 October 2012

Keywords:
New Zealand
Southern Alps
Palaecoclimate
Glacier modelling
Lateglacial
Antarctic cold reversal

Abstract
Climate proxy records from the middle to high latitude Southern Hemisphere indicate that a Lateglacial (15,000–11,500 years ago) climate reversal, approximately coeval with the Antarctic Cold Reversal (ACR), interrupted a warming trend during deglaciation. In New Zealand, some palaecoclimate proxy records indicate a cool episode during the ACR (ca 14,500–12,500 years ago), while others do not express a significant change in climate. Recently published moraine maps and ages present an opportunity to improve the palaecoclimate interpretation through numerical modelling of glaciers. We use a coupled energy-balance and ice-flow model to quantify palaecoclimate from past glacier extent constrained by mapped and dated moraine crests in the headwaters of Irishman Stream, a high-elevation catchment in the Southern Alps. First, a suite of steady-state model runs is used to identify the temperature and precipitation forcing required to fit the modelled glacier to well-dated Lateglacial moraine crests. Second, time-dependent glacier simulations forced by a nearby proxy temperature record derived from chironomids are used to assess the fit with the glacial geomorphic record. Steady-state experiments using an optimal parameter set demonstrate that the conditions under which the 13,000 year old moraine formed were 2.3–3.2 °C colder than present with the range in temperature corresponding to a ±20% variance in precipitation relative to the present-day. This reconstructed climate change relative to the present-day corresponds to an equilibrium-line altitude of ca 2000 ± 40 m above sea level (asl), which is ca 400 m lower than present. Time-dependent simulations of glacier length produce ice advance to within 100 m of the 13,000 year old terminal moraine, indicating that the chironomid-based temperature forcing and moraine record provide consistent information about past climate. Our results, together with other climate proxy reconstructions from pollen records and marine sediment cores, support the notion that temperatures during the ACR in New Zealand were ~2–3 °C cooler than today.

1. Introduction

During the Lateglacial interval (~15,000–11,500 years ago or 15–11.5 ka) in the middle to high latitudes of the southern hemisphere, a warming trend was interrupted by the Antarctic Cold Reversal (ACR, ~14.5–12.5 ka (EPICA Community Members, 2006)). New Zealand is one of the few locations in the southern middle latitudes where Lateglacial moraines exist. Many examples
of Lateglacial moraines in the Southern Alps of New Zealand have been identified (Porter, 1975b; Suggate, 1990; Fitzsimons, 1997), mapped (Birkeland, 1982; Barrell et al., 2011), and some have been dated (e.g., Turney et al., 2007; Kaplan et al., 2010; Putnam et al., 2010). Transformation of glacier fluctuation records to climate changes is not a trivial process due to several non-climatic influences and is not readily achievable for some types of glacier (e.g., debris-covered or calving (Winkler et al., 2010; Anderson and Mackintosh, 2012; Chinn et al., 2012)). Porter (1975a) estimated that the Lateglacial equilibrium-line altitude (ELA) in the Tasman River catchment was 500 ± 50 m lower than modern, based on an accumulation area ratio (AAR) analysis of reconstructed glaciers inside the Birch Hill moraine limit. Other proxy records rarely afford quantitative climate estimates. Besides glacial deposits, records that show a prominent cooling during the Lateglacial include sea surface temperature reconstructions from around New Zealand (Pahnke et al., 2003; Barrows et al., 2007; McGlone et al., 2010), pollen records from upland locations in New Zealand (Burrows and Russell, 1990; McGlone, 1995; Newnham and Lowe, 2000; Turney et al., 2003; McGlone et al., 2004; Vandergoes et al., 2008), and chironomid-derived temperature reconstructions (Vandergoes et al., 2008). Less pronounced climate reversals within or overlapping with the ACR period have also been inferred based on other pollen (Newnham et al., 2007, 2013) and speleothem (Williams et al., 2005) records (see also Alloway et al. (2007)). In this paper, we aim to improve our understanding of the Lateglacial climate event in New Zealand using glacier modelling techniques.

1.1. Glaciers as a climate proxy

Glacier extent depends on the balance between accumulation and ablation (Oerlemans, 2001, 2005). Moraine positions in mountainous regions provide evidence of former glacier extents and may be used to infer past climates. Glacial geomorphic mapping of the central South Island of New Zealand (Barrell et al., 2011) has yielded a high-quality constraint on past ice extents, and several surface exposure dating studies provide ages for the culmination of Lateglacial ice advances (Ivy-Ochs et al., 1999; Kaplan et al., 2010; Putnam et al., 2010).

We present an application of a 2-D ice-flow and energy mass-balance model (EBM) to reconstruct temperature and precipitation values for the ACR. We apply these models to a glacier whose extent is delineated by moraines mapped by Kaplan et al. (2010) in the headwaters of Irishman Stream in the central Southern Alps of New Zealand and compare our findings to their AAR reconstructions and other climate proxy records. In experiment 1, we explore the different combinations of temperature and precipitation required to produce a steady-state glacier that most closely matches the moraine record, taking account of uncertainties associated with model parameter choices. In experiment 2, we use a chironomid-derived temperature reconstruction (Vandergoes et al., 2008) to drive our glacier model and test if this climate forcing produces ice extents compatible with the moraine record (Kaplan et al., 2010).

1.2. Study area

The South Island of New Zealand is dominated by the high axial range of the Southern Alps, which impedes the prevailing westerly winds, resulting in a steep west to east precipitation gradient (Griffiths and McSaveney, 1983; Henderson and Thompson, 1999). Glaciers with fast response times to climate perturbations are abundant in the central Southern Alps due to high snowfall rates and steep mountain slopes (Chinn, 1996; Fitzharris et al., 1999). We focus on moraines deposited in the headwaters of Irishman Stream (43°59′30″S, 170°03′00″E), located in the Ben Ohau Range (Fig. 1) (McGregor, 1967; Birkeland, 1982; Kaplan et al., 2010). The dated glacial deposits lie at the edge of a cirque, referred to here as Irishman basin, that comprises the upper 2 km of Irishman Stream.

Fig. 1. Location of the study area in central South Island, New Zealand. The Ben Ohau Range is outlined in green and Irishman basin is in the white box. Boundary Stream tarn (BST) is represented by the white dot southeast of Irishman basin and the white triangles are the locations of Aoraki/Mt. Cook village (north of the Ben Ohau Range) and Twizel (southeast of Ben Ohau Range). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
valley. The basin floor, for the most part, slopes gently (~15°) towards the southwest.

Aside from the mapped and dated moraine sequence, there are several reasons why Irishman basin is well-suited for this study. First, Irishman basin is located <30 km to the southeast of the most glaciated section of the Southern Alps and is affected by the same regional atmospheric circulation, including the prevailing westerly winds (Kaplan et al., 2010; Chinn et al., 2012). Second, Irishman basin lacks complex terrain and has a shallow gradient, making our use of the shallow ice approximation equations an appropriate model choice (Leyssinger Vieli and Gudmundsson, 2004). Third, the basin supported a single glacier with no tributaries, making it a very simple glacier system for ice reconstructions. Fourth, the present-day digital elevation model provides an appropriate topographic boundary condition for the numerical model because the basin is presently ice-free, and the visible bedrock knobs and outcrops on the valley floor indicate little sediment accumulation and hence minor topographic change since deglaciation. Moreover, the 15° down-valley slope of the basin floor precludes the former existence of large proglacial lakes and calving ice termini. Therefore, we assume glacier fluctuations in this valley directly relate to changes in atmospheric conditions and hence climate over this part of the South Island.

There are several reasons why we believe that the Irishman basin glacier at 13 ka did not contain a significant surface debris cover. Although there are rock glaciers at the headwalls of Irishman basin and the basin has a veneer of rock debris, through which bedrock hills are visible, the Late-glacial moraine is not particularly large, especially the left lateral segment (Kaplan et al., 2010). These features suggest that debris cover of past glaciers in this valley was not sufficient to dramatically affect the albedo/energy balance. Also, present-day Glenmary Glacier, 12 km west of Irishman basin, is an example of a small cirque glacier in a similar setting to that of the 13 ka Irishman glacier that is relatively free of debris-cover.

There are no long-term climate data from Irishman basin. We characterised the present climate by interpolating between data from multiple low-elevation stations and measurements from a temporary climate station that we installed in Irishman basin (43°59’30”S, 170°2’57”E, 2010 m a.s.l.). The station operated over an 11 month period, March 2010—January 2011, so February values are inferred to be the same as January temperature values to calculate an annual mean temperature of 1.2 °C. Hourly temperatures from the temporary station were averaged into monthly mean temperatures (Table 1), with the warmest month at 6.2 °C (January, 2011) and the coolest month at ~6.1 °C (June, 2010).

Interpolated precipitation data suggest an annual mean of 1240 mm (Stuart, 2011) for this location. Although the annual total precipitation surface and monthly mean interpolated precipitation data are based on data from many long-term rain gauges located in the central Southern Alps, we use two nearby stations to provide an indication of precipitation variation at Irishman basin. Mean precipitation data from Twizel, 30 km to the south (Station numbers 4995, 4996, 4997), from 1973 to 1997 is ~610 mm a⁻¹ with a standard deviation of ±110 mm a⁻¹ (18%) (National Institute for Water and Atmospheric Research (NIWA), Retrieved 2009–2011). Likewise, mean precipitation data from Aoraki/Mt. Cook village, 30 km to the north (Station numbers 18125, 4591, 4593), from 1930 to 2011 is ~4100 mm a⁻¹ with a standard deviation of ±900 mm a⁻¹ (22%) (NIWA, Retrieved, 2009–2011) (Twizel and Aoraki/Mt. Cook village locations are shown in Fig. 1). We consider the characteristic present-day precipitation variability to be ~20%, based on the standard deviation from these stations.

2. Modelling glacier extent

We used a simple iterative modelling approach to estimate palaeoclimate conditions based on modelled glacier extent. This strategy is similar to those employed in previous studies (Plummer and Phillips, 2003; Hubbard et al., 2005; Kessler et al., 2006; Laabs et al., 2006) except that our 2-D ice-flow model is coupled with a spatially-distributed EBM. Our EBM/2-D ice-flow combination is simple enough to simulate mapped ice extents quickly (steady-state runs take less than an hour on a desktop computer), yet it is complex enough to account for shading, aspect, valley slope, and local climate.

A digital elevation model was used to provide surface elevation throughout the model domain. This model was produced from 20 m interval topographic contours and spot heights on published 1:50,000-scale (NZMS260 series) topographic maps published by Land Information New Zealand. We simulated the 13 ka Irishman glacier at 25 × 25 m gridded horizontal resolution, with all simulations starting from an ice-free basin. The model domain covers a 5 × 6 km area centred over Irishman basin.

2.1. Input data

Thirty years (1981–2010) of daily climate data were converted into monthly means for each grid cell in the model domain. We calculated climate data grids from several different sources depending on availability and reliability. First, daily climate data of relative humidity, solar radiation, temperature, and precipitation came from the NIWA CliFlo Database (NIWA, Retrieved, 2009–2011). Relative humidity and solar radiation grids came from the virtual climate station network climate grid interpolations, available directly from the NIWA CliFlo website. The NIWA climate grids were not used for temperature because the data contain some biases in mountainous terrain (Anderson and Mackintosh, 2012). Instead, we created interpolated temperature surfaces using data from multiple, surrounding, low-elevation stations (NIWA, Retrieved, 2009–2011). To make the interpolation surface, we took daily temperature data from each station (Tₑ in °C), the monthly lapse rate (dT/dz in °C km⁻¹), and station elevation (zₑ in m) to create a ‘reference’ temperature (Tᵣ in °C) at sea level using:

\[ Tᵣ = Tₑ - \frac{dT}{dz} zₑ \]  

(1)

Daily reference temperature surfaces were interpolated at sea level in the horizontal plane across the model domain (Tait and Zheng, 2007). Modelled temperature (T in °C) in any grid cell was calculated using Equation (2), with the grid cell reference temperature, the month’s lapse rate, and the elevation value of the grid cell (z in m). Each modelled past temperature change (ΔT) is an additive change to the temperature (T) in each grid cell and is uniformly applied across the domain:

<table>
<thead>
<tr>
<th>Month</th>
<th>Jan</th>
<th>Feb</th>
<th>Mar</th>
<th>Apr</th>
<th>May</th>
<th>Jun</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tₑ [°C]</td>
<td>6.2</td>
<td>4.9</td>
<td>3.1</td>
<td>3.1</td>
<td>3.1</td>
<td>6.1</td>
</tr>
<tr>
<td>dT/dz [°C km⁻¹]</td>
<td>-6</td>
<td>-6</td>
<td>-5.5</td>
<td>-5.5</td>
<td>-5</td>
<td>-4</td>
</tr>
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<tr>
<th>Month</th>
<th>Jul</th>
<th>Aug</th>
<th>Sep</th>
<th>Oct</th>
<th>Nov</th>
<th>Dec</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tₑ [°C]</td>
<td>-6</td>
<td>-3.6</td>
<td>-1.5</td>
<td>0.8</td>
<td>4.9</td>
<td>6</td>
</tr>
<tr>
<td>dT/dz [°C km⁻¹]</td>
<td>-3.5</td>
<td>-5.5</td>
<td>-6.5</td>
<td>-5.5</td>
<td>-5.5</td>
<td>-6</td>
</tr>
</tbody>
</table>

* The February dT/dz was set equal to the January value because of a data gap.
We developed a spatially-distributed EBM that uses the specified topography, monthly interpolated meteorological input, ice thickness at each monthly time-step, and prescribed climate perturbations to calculate annual mass balance at each grid cell. The resulting mass balance grid was then used as a boundary condition in our ice-flow model (Section 2.3). Several other workers have employed 1- and 2-D models based on similar sets of equations (e.g., Oerlemans, 1992; Plummer and Phillips, 2003; Hock, 2005). We followed an EBM scheme described in Anderson et al. (2010) and Anderson and Mackintosh (2012), except ours used a monthly timestep and updates mass balance once every 5 or 20 model years (transient and steady-state respectively). The model calculated the energy available for melt ($Q_m$) using the following equation:

$$Q_m = I(1 - \alpha) + L_i + L_t + Q_H + Q_c + Q_e + Q_R$$

where $I$ is the incoming shortwave radiation, $\alpha$ is the surface albedo, $L_i$ is the incoming longwave radiation, $L_t$ is the outgoing longwave radiation, $Q_H$ and $Q_c$ are the sensible and latent heat fluxes, $Q_e$ is the ground heat flux, and $Q_R$ is the heat supplied by rain. All heat exchanges are in units of W m$^{-2}$. Positive values of radiative and turbulent fluxes indicate a gain of energy for melting of the snowpack, and negative values indicate a loss of energy. $Q_e$ was set at 1 W m$^{-2}$ (Neale and Fitzharris, 1997) and $Q_R$ was calculated assuming that precipitation is the same temperature as the air (Oerlemans, 1992).

Incoming shortwave radiation ($I$) was comprised of direct and diffuse components following Oerlemans (1992). Cloudiness (see above) was included in the insolation calculations following Hock (2005) and Anderson et al. (2010). Insolation values for the steady-state simulations were calculated for 13 ka (Berger and Loutre, 1991; Eisenman and Huybers, 2006). The albedo parameterisation ($\alpha$) was based on a background albedo profile, which shows albedo increasing with altitude and snow thickness, both dependent on the modelled ELA, following Oerlemans (1992). Longwave and shortwave radiation distribution were calculated to include the view field of the surrounding topography from the cell and cloudiness following Plummer and Phillips (2003) and Anderson et al. (2010). Turbulent heat fluxes ($Q_h$ and $Q_c$), which can make up half or more of the energy available for melt in maritime environments (Anderson and Mackintosh, 2012), were calculated using the bulk method (Klok and Oerlemans, 2002; Oerlemans and Grisogono, 2002) following Oerlemans (1992). The turbulent heat calculations used different roughness lengths for snow and ice surfaces and the Richardson stability criterion was applied for stable stratification conditions (Oerlemans, 1992; Hock, 2005; Anderson et al., 2010).

Snow accumulation occurred in the model when the temperature at each grid cell was at or below a snow/rain temperature threshold. The snow temperature threshold ($T_s$) was set to 1 °C (Anderson et al., 2006). We did not take possible surface debris cover effects into account in these palaeo-simulations, although this cover was likely insignificant when Irishman glacier filled much of the basin at the ACR extent as suggested by the present geomorphology and previous glacier reconstructions (Kaplan et al., 2010).

Mass balance of the simulated glacier was calculated by subtracting the mass of possible melt from the mass of snow accumulation at each grid cell. The mass balance was recalculated every 20 model years in steady-state runs (every 5 model years in transient runs). The mass balance was pre-defined at zero, and therefore no mass was added to the glacier at the start of each run. The mass balance grid was then used as a boundary condition in our ice-flow model.

The first source of input climate data came from the first source of input climate data came from the National Centers for Environmental Prediction (NCEP) for present-day wind at the 850 hPa level (1981–2010) (Kalnay et al., 1996) were scaled to match observed wind speed and were applied uniformly across the model domain. Wind speeds are not modified for the complex topography and we assume wind speed distribution is uniform over the domain. These data were converted into monthly mean gridded wind speed. Further discussion of these datasets and the rationale for using them is provided in Anderson and Mackintosh (2012).

The second source of input climate data came from an annual mean precipitation surface (Stuart, 2011) based on rain gauge data, from 1971 to 2000, spatially distributed around the Southern Alps to capture the steep precipitation gradient. The interpolated precipitation (Anderson et al., 2010) amount at each grid cell was calculated at monthly mean values from daily measured rainfall at lowland stations (NIWA). The interpolated data were guided by an annual mean precipitation surface (Stuart, 2011).

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We used the following equation to calculate precipitation:

$$P = \frac{dP}{dz}$$

where $P$ is the precipitation, $z$ is the height, and $\Delta P$ is the change in precipitation reaching the site, which could be a result of regional changes in annual precipitation and/or changes in the amount of snow settling within Irishman basin as a result of increasing or decreasing snow transport.

### 2.2. The energy-balance model

We developed a spatially-distributed EBM that uses the specified topography, monthly interpolated meteorological input, ice thickness at each monthly time-step, and prescribed climate perturbations to calculate annual mass balance at each grid cell. The resulting mass balance grid was then used as a boundary condition in our ice-flow model (Section 2.3). Several other workers have employed 1- and 2-D models based on similar sets of equations (e.g., Oerlemans, 1992; Plummer and Phillips, 2003; Hock, 2005). We followed an EBM scheme described in Anderson et al. (2010) and Anderson and Mackintosh (2012), except ours used a monthly timestep and updates mass balance once every 5 or 20 model years (transient and steady-state respectively). The model calculated the energy available for melt ($Q_m$) using the following equation:

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transient runs) while the ice-flow model ran. Coupling the models allowed the parameters sensitive to topography or the presence of ice (i.e., albedo, turbulent heat fluxes, shading, longwave radiation) to readjust as the ice thickness and extent evolved.

2.3. The ice-flow model

The ice-flow model employed in this study is a 2-D shallow ice approximation model, with an explicit time-step, similar to Plummer and Phillips (2003) and Kessler et al. (2006). The model used the basic mass continuity equation:

\[
\frac{dH}{dt} = M - \nabla \cdot \bar{q}
\]  

(4)

where \(H\) is the ice thickness, \(t\) is time, \(\bar{q}\) is ice flux, and \(M\) is the mass balance, which was calculated using the EBM described in Section 2.2. The flux divergence was calculated using a 2-D finite-difference scheme. The vertically-averaged ice velocity from internal deformation was calculated using the shallow ice approximation (Paterson, 1994):

\[
\bar{U}_d = \frac{2}{5} A H \bar{\tau}_b^n
\]  

(5)

where \(A\) is the coefficient of Glen’s flow law, set to \(1 \times 10^{-17} \text{ Pa}^{-3} \text{ a}^{-1}\), \(\bar{\tau}_b\) is the gravitational driving stress (\(\bar{\tau}_b = \rho g H \bar{\tau}_z\)), and \(n\) is Glen’s flow law exponent, set to 3. The sliding velocity follows the empirical formulation of Kessler et al. (2006):

\[
\bar{U}_s = U_c e^{-\frac{\tau_c}{\bar{\tau}_b}}
\]  

(6)

where \(U_c\) is a typical sliding velocity (20 m a\(^{-1}\)) and \(\tau_c\) is the gravitational driving stress (10\(^5\) Pa) that results in \(\bar{U}_s\).

The continuity equation (Equation (4)) was used to evolve the glacier geometry through time by calculating the ice velocity (\(\bar{U}_d + \bar{U}_s\)).

Fig. 3. Modelled extent of Irishman glacier at 13 ka where \(\Delta T - 2.5 \degree C\) and \(\Delta P + 11\%\). We show the (a) mapped geomorphology in the Irishman basin, for details see Kaplan et al. (2010), (b) modelled ice thickness overlaying the moraine map, (c) modelled mass balance with modelled ELA (green dashed line), and (d) previous estimates of Irishman glacier extent (K1 blue, K2 red) and ELA (K1ELA blue dashed, K2ELA red dashed) (Kaplan et al., 2010) based on geometric and AAR reconstructions, compared to this study (green). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
Irishman glacier while it is in equilibrium (where the rate. The integrated mass balance over the glacier surface, for the modelled glacier in equilibrium relative to the total accumulation of the updated ice thickness using a forward explicit time-step. The model is to adjust to equilibrium starting from ice-free conditions. The EBM ran to modern day (after 13 ka). The glacier overall has a low aspect ratio and a low ice surface gradient. We consider the primary control on glacier evolution in Irishman basin to be the mass balance (Le Meur et al., 2004), however, Irishman glacier overall has a low aspect ratio and a low ice surface gradient. We assume that the glacier was in equilibrium with the climate when it deposited the moraine. Each steady-state simulation ran for 240 model years, which is greater than the time scale on that curve produced the moraine position. In the Lateglacial time (Vandergoes et al., 2008) (Fig. 1). The age model at the BST site is derived from Bayesian modelling of 17 radiocarbon dates, calibrated using IntCal04 (Vandergoes et al., 2008). The chironomid record shows a period of temperature instability between 14.2 and 13.2 ka, including a maximum cool spike between 2 and 3 °C below present values (Vandergoes et al., 2008). Particular strengths of the BST record are that chironomids are sensitive to mean summer temperatures (Dieffenbacher-Krall et al., 2007), the site lies close to Irishman basin, and the chironomid record is compatible with pollen-based palaeoclimate proxies from the same core. Although the chironomid temperature reconstruction describes mean summer temperature values, we apply it to our model as mean annual temperature changes. The sample specific error on the chironomid-derived temperatures is ±1.4 °C. Vandergoes et al. (2008) reconstructed summer temperatures from chironomids using two different modern-day chironomid-temperature calibration models and published both the raw and smoothed data from these models. They drew their conclusions (as much as 2–3 °C cooling during the ACR) from once every 20 model years to recalculate the glacier mass balance. These simulations used values from our optimal parameter set (Table 2).

In order to assess the impact of parameter choices on our results, the following parameters were systematically explored: T, αsnow, Zice, Zsnow, Uice, A, and A. In each case the model ran using the optimal parameter set with the exception of the parameter we were testing. These tests were done with a similar model setup to experiment 1, each running for 240 model years, changing ΔP – ΔT combinations until the glacier reached within 50 m of the moraine. In the sensitivity tests, we created a new ΔP – ΔT curve for each tested parameter (Fig. 4).

### 2.5. Transient runs

In experiment 2, transient model runs were forced using chironomid-derived mean summer temperature reconstructions from sediments at Boundary Stream tarn (BST, 44°02’S, 170°07’E, 830 m asl) located 7 km southeast of Irishman basin, that span the Lateglacial time (Vandergoes et al., 2008) (Fig. 1). The age model at the BST site is derived from Bayesian modelling of 17 radiocarbon dates, calibrated using IntCal04 (Vandergoes et al., 2008). The chironomid record shows a period of temperature instability between 14.2 and 13.2 ka, including a maximum cool spike between 2 and 3 °C below present values (Vandergoes et al., 2008). Particular strengths of the BST record are that chironomids are sensitive to mean summer temperatures (Dieffenbacher-Krall et al., 2007), the site lies close to Irishman basin, and the chironomid record is compatible with pollen-based palaeoclimate proxies from the same core. Although the chironomid temperature reconstruction describes mean summer temperature values, we apply it to our model as mean annual temperature changes. The sample specific error on the chironomid-derived temperatures is ±1.4 °C. Vandergoes et al. (2008) reconstructed summer temperatures from chironomids using two different modern-day chironomid-temperature calibration models and published both the raw and smoothed data from these models. They drew their conclusions (as much as 2–3 °C cooling during the ACR) from

![Fig. 4. Experiment 1 results: Inferred ΔP – ΔT reconstructions showing the sensitivity of the climate reconstruction to chosen parameter values. Curves identical to the ‘Optimal’ curve are not shown (I, U, A, and Zice = 0.002 m). The x-intercepts of the different curves are reported in Table 3.](image)
the smoothed data of the partial least squares (PLS-smooth) model. We used all four temperature reconstructions (PLS-raw, PLS-smooth, weighted average partial least squares (WAPLS)-raw, and WAPLS-smooth) to drive our EBM/2-D ice-flow model ∆T values. Each simulation was compared to the moraine sequence dated by Kaplan et al. (2010) to determine the best fit out of the four temperature reconstructions.

Temperatures were interpolated between the data points in each reconstruction from Vandergoes et al. (2008) using nearest neighbour interpolation. Precipitation was set to 0% change (present-day) for all transient runs. Each simulation ran for 4000 model years (15–11 ka) and the EBM ran once every 5 model years to recalculate the energy balance on the evolving ice surface including differences in insolation (I) due to changing orbital parameters during the period 15–11 ka.

3. Results

3.1. Experiment 1: steady-state simulations of the ACR Irishman glacier extent

The first experiment of our investigation involved carrying out a suite of equilibrium runs at set ∆P = ∆T combinations to identify those that produced a good match with the Irishman basin 13 ka moraine position (Fig. 3a and b). Fig. 3b shows the fit between modelled ice thickness and the moraine record during a single simulation where ∆T is −2.5 °C and ∆P is +11%. The modelled Irishman glacier at the 13 ka extent has an area of ~1.8 km², volume of ~0.015 km³ and a maximum thickness of 100 m. The modelled glacier response time to a 1 °C decrease in ∆T is 10² model years, suggesting that the glacier would respond to centennial scale shifts in climate, rather than decadal. The relatively long response time is consistent with the low slope angle of Irishman basin and a relatively low mass turnover.

Fig. 3c shows the mass balance of Irishman glacier when ∆T is −2.5 °C and ∆P is +11%. Mass balance ranges from 1 m w.e. accumulation at highest elevations to −2 m w.e. ice melt at the terminus. The modelled ELM (mean elevation where mass balance equals zero) in this simulation is 2000 ± 40 m asl. The present-day ELM is above the elevation of Irishman basin and has been extrapolated to >2300 m asl from present-day glacier snowlines (Porter, 1975b; Chinin, 1995; Lamont et al., 1999; Mathieu et al., 2009). To assess this estimate and to compare our palaeo-ELA with that of today, we applied the same climate data interpolation scheme and energy balance model to an idealised, cone-shaped and ice-covered mountain rising to 2500 m asl at the same location as Irishman basin. The modelled present-day ELM for Irishman basin derived using this method is ~2400 ± 40 m asl, only ~100 m above the highest points of the headwall of Irishman basin. Therefore, the ELM lowering that corresponds to the ACR event is ~400 ± 40 m.

Fig. 4 displays the ∆P − ∆T curves using the optimal parameter set (Table 2) and variations in parameters. A similar glacier geometry to that shown in Fig. 3b will form with any ∆P − ∆T combination on the black curve in Fig. 4, although the glaciers resulting from a larger precipitation increase are slightly thicker. With no change in temperature, a precipitation increase of 241% is necessary to simulate the moraine position (not shown in Fig. 4).

Varying the Tₑ and αsnow individually has the largest impact of all parameters on our climate results. Changes of ±1 °C in the Tₑ alone influences the temperature reconstruction by ±0.3 °C. Likewise, changing the αsnow alone by ±0.05 modifies ∆T by ±0.6 °C. Despite the effects of parameter choice on our climate reconstructions, the overall conclusions do not change. Variations in other parameters have smaller influences on the ∆P − ∆T curve. For example, varying the local summer insolation (I) between low (18 ka) and high (10 ka) values makes no direct difference in the modelled glacier extent or climate reconstruction.

Table 3 lists the parameters, the values used in the sensitivity tests, and the ∆T needed to grow the glacier to the 13 ka moraine without a change in precipitation (x-intercept), with the optimal parameter set yielding a ∆T of −2.7 °C.

### Table 3

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
<th>∆T (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Snow albedo</td>
<td>αsnow</td>
<td>0.67</td>
<td>−3.3</td>
</tr>
<tr>
<td>Snow/rain temperature threshold (°C)</td>
<td>Tₑ</td>
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<td>Temperature lapse rate (°C km⁻¹)</td>
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<td>−3.0</td>
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<tr>
<td>Roughness parameter for ice (m)</td>
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<td>−2.7</td>
</tr>
<tr>
<td>Roughness parameter for snow (m)</td>
<td>Zsnow</td>
<td>0.0005</td>
<td>−2.7</td>
</tr>
<tr>
<td>Incoming shortwave radiation (ka)</td>
<td>I</td>
<td>10</td>
<td>−2.7</td>
</tr>
<tr>
<td>Typical sliding velocity (m a⁻¹)</td>
<td>Uₑ</td>
<td>18</td>
<td>−2.7</td>
</tr>
<tr>
<td>Glen's flow law coefficient (Pa⁻³ a⁻¹)</td>
<td>A</td>
<td>1e⁻¹⁶</td>
<td>−2.7</td>
</tr>
</tbody>
</table>

3.2. Experiment 2: transient run driven by chironomid-derived temperature reconstructions

The second experiment of our study was to run four time-dependent simulations of glacier extent forced by the different BST chironomid-derived temperature reconstructions (Vandergoes et al., 2008). The resulting glacier length changes were then compared with the mapped and dated moraine sequence in Fig. 3a. Fig. 5 shows the PLS-smooth BST ∆T (present-day temperature is ∆T = 0 °C) from 15 to 11 ka, and the lower plot shows the corresponding change in glacier length. The 13 ka moraine position (in terms of glacier length) is represented on Fig. 5 by the orange diamond with the error bars corresponding to the age of the moraine derived independently using surface exposure dating by Kaplan et al. (2010).

From 15 to 14 ka, temperature in the PLS-smooth chironomid model varies between +0.5 and −2.5 °C relative to the present. In response to this temperature forcing, the modelled glacier fluctuates between a length of 1640 m (about 100 m short of the moraine) and ice-free conditions. Ice persists at the headwall with a ∆T = −1 °C, which supports our modern ELA estimate and the regional interpretation that the modern ELA lies just above the highest parts of the Irishman basin headwall (Porter, 1975b; Brazier
et al., 1998; Lamont et al., 1999). The modelled glacier almost reaches the position of the 13 ka moraine in response to the short-term 2.8 °C cooling at 13.8 ka and retreats to within 250 m of the headwall by 13.3 ka after a change in ΔT from −2 to −1 °C. Subsequent ice advances from 13.5 to 11 ka are minor (<250 m) in the model run. The PLS-smooth forcing does not produce ice extents coinciding with the 12 ka and 11.5 ka moraines of Kaplan et al. (2010) (Fig. 5, represented by the yellow diamond and error bars).

All other BST temperature reconstructions produced modelled glacier extents (not shown) far beyond the moraine position during the coldest part of the curve, leading to a mismatch with the moraine data. PLS-raw data included a maximum ΔT of −4 °C, resulting in a modelled glacier length of 3000 m, almost twice the geomorphically delimited length. WAPLS-raw and WAPLS-smooth included a maximum ΔT of −5.6 and −4.4 °C respectively and both produced valley glaciers that were too extensive (~5500 m long). Model simulations with a greater magnitude of cooling, such as WAPLS-raw and WAPLS-smooth, also produced ice on the valley wall sides, which is not supported by the geomorphic evidence.

4. Discussion

We sought to improve Lateglacial palaeoclimate estimates derived from glacier reconstructions for central South Island by using a numerical modelling approach. Although this reconstruction is for a single site, ice in the Irishman basin would have responded to the same regional climatic changes as other glaciers in the central Southern Alps (Clare et al., 2002; Kaplan et al., 2010; Chinn et al., 2012). There is no present-day glacier in Irishman basin, and as a result we do not have site specific mass balance measurements with which to compare our results against directly, thereby tuning the model to this site. We do use temperature data from an automatic weather station setup in Irishman basin to determine appropriate seasonal lapse rates. The modelled 'equilibrium-line altitude' is above the ridge elevation, which is similar to previously interpolated ELAs (Chinn, 1995). Moreover, the model has been tuned and tested for other New Zealand glaciers (Anderson et al., 2010; Anderson and Mackintosh, 2012).

At present, Irishman basin has an annual mean temperature of ~1.2 °C, and a cooling of only 1 °C results in small glaciers developing at the headwall, which suggest that this site is ideal for recording even minor past shifts in climate. Our model successfully reproduced ice extent matching the moraine record with an estimated ΔT of −2.7 ± 0.6 °C, which supports previous evidence of a cold event in New Zealand during the ACR (e.g., Porter, 1975a; Hajdas et al., 2006; Carter et al., 2008; Putnam et al., 2010). There are a number of model parameter values that are uncertain for palaeoclimate simulations (Table 2) and we presented their effect on the modelling results (Fig. 4).

Ice extent and ELA reconstructions using the AAR method from Kaplan et al. (2010) are compared to our modelled ice extent and ELA in Fig. 3d. Our modelled area extent (1.8 km²) matches more closely with the smaller ice reconstruction (K1), whereas our model-based ELA estimate of 2000 ± 40 m asl is closer to the larger reconstruction (K2), which gave an ELA of 1980 ± 40 m asl. This is because the AAR (automatically) calculated by the mass balance model was 0.58, compared to the 0.67 assumed by Kaplan et al. (2010). However, within uncertainties, all three reconstructions yield identical or similar extents, ELAs, and ice thicknesses. The agreement between the methods supports the use of the AAR method on glaciers in a simple topographic context with a well expressed geomorphic moraine record. Our estimated ELA lowering from the present day is ~400 m for Irishman basin, which is similar to the ELA lowering derived for the Birch Hill event (500 m) in the Tasman valley (Porter, 1975a), which is also dated to 13.1 ka (Putnam et al., 2010).

The transient simulations, using BST temperatures and moraine age and position as constraints, show an advance/retreat pattern in Irishman glacier from 15 to 11 ka. The modelled glacier advances to within 100 m of the moraine during the BST cold period (ΔT = −2 to −3 °C between 13.9 and 13.4 ka) and retreats to within 240 m of...
the headwall when the BST ΔT increases to $-1{^\circ}C$ ($\sim 13.3$ ka). The 2–3 $^\circ$C cooling persisting for $\sim 500$ years from the chironomid record is sufficient to grow Irishman glacier out to the 13 ka moraine. The timing of the simulated glacier retreat overlaps within error with the moraine age ($13 \pm 0.5$ ka) (Fig. 5). A poorer match, however, is achieved for the 12 and 11.5 ka moraines, where the simulated glacier extent is $\sim 500$ m from the 12 ka moraine. This mismatch occurs because the BST temperature decrease is not of sufficient magnitude to produce the inferred glacier extent. The 12 ka temperature decrease might not be appropriately captured in the BST record due to lower sampling resolution during that time.

Overall, we see a good match between the chironomid-derived temperature reconstruction and the ACR moraine position via our modelling results. The brief cool spike from the PL2-smooth (Fig. 5) results in a glacier extent near the moraine, but predates the moraine age. Small mismatches in the chironomid and moraine records may reflect model, moraine dating, or BST age-model uncertainties, but could also reflect differences in response of each proxy to climate. We point out that chironomid- and glacier-derived palaeoclimate records are inherently different, because they respond on different timescales and, perhaps, emphasise different characteristics of temperature change (e.g., tann temperature versus glacier micro-climate). Yet, despite potential differences, these proxies both appear to be predominantly reflecting changes in temperature of approximately the same magnitude during the ACR.

The modelling results presented in this paper supports the idea that the temperature during the ACR was 2–3 $^\circ$C cooler than today in New Zealand. This temperature change estimate overlaps, within error, with a temperature change estimate of 3–4 $^\circ$C cooler than today, reported by Anderson and Mackintosh (2006) for the Franz Josef Glacier advance to the Waiho Loop during the Lateglacial. Our results are also consistent with published pollen studies (Newnham and Lowe, 2000; T urney et al., 2003; Vandergoes and Fitzsimons, 2003; Hajdas et al., 2006), and regional sea-surface temperature records (Carter and Cortese, 2009; Sikes et al., 2009) that suggest a temporary reversal of the deglaciation warming trend occurred in New Zealand during the Lateglacial.

5. Conclusions

We simulated a small glacier in the central Southern Alps to infer the local climate change that occurred during the ACR using a coupled energy-balance and ice-flow model. We show that:

1. Our simulated equilibrium-line altitude is 2000 $\pm$ 40 m asl, which agrees within error with the traditional AAR method of reconstruction (1980 $\pm$ 40 m asl (Kaplan et al., 2010)). Our estimated Lateglacial ELA is 400 m lower than the modelled modern ELA of 2400 $\pm$ 40 m.

2. A ΔT (temperature change from today) of $-2.7 \pm 0.6$ $^\circ$C was required to simulate the ACR extent of Irishman glacier assuming no change in precipitation from present day.

3. The optimal parameter set curve shows a ΔT of $-2.3$ $^\circ$C when $\Delta P$ (precipitation change from today) is $-20\%$ and $-3.2$ $^\circ$C when $\Delta P$ is $-20\%$.

4. The transient simulation of Irishman glacier length from 15 to 11 ka, driven by a chironomid-derived temperature reconstruction (Vandergoes et al., 2008), showed advance to and retreat from the 13 ka moraine.

5. Our model-based temperature reconstructions are compatible with other proxy records from New Zealand that show temperatures during the ACR were cooler than today.

Acknowledgements

Funding was provided by the New Zealand Government under a New Zealand International Research Doctoral Scholarship, by the Comer Science and Education Foundation and by Victoria University of Wellington, including the Antarctic Research Centre, the School of Geography, Environment and Earth Sciences, and the Science Faculty Research Committee. M. Vandergoes and D. Barrell were supported by GNS Science’s Direct Crown Funded Programme ‘Global Change through Time’. We thank S. Stuart for providing his Southern Alps precipitation surface and R. Dadic, N. Golledge, H. Horgan, and K. Sattler for helpful discussions during the preparation of this paper. We also appreciate the helpful comments from M. Plummer and an anonymous reviewer. This publication is LDEO contribution number 7618.

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